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Amplitude analysis of $B^0 \rightarrow \bar{D}^0 K^+ \pi^-$ decaysR. Aaij *et al.**

(LHCb Collaboration)

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The Dalitz plot distribution of $B^0 \rightarrow \bar{D}^0 K^+ \pi^-$ decays is studied using a data sample corresponding to 3.0 fb^{-1} of pp collision data recorded by the LHCb experiment during 2011 and 2012. The data are described by an amplitude model that contains contributions from intermediate $K^*(892)^0$, $K^*(1410)^0$, $K_2^*(1430)^0$ and $D_2^*(2460)^-$ resonances. The model also contains components to describe broad structures, including the $K_0^*(1430)^0$ and $D_0^*(2400)^-$ resonances, in the $K\pi$ S-wave and the $D\pi$ S- and P-waves. The masses and widths of the $D_0^*(2400)^-$ and $D_2^*(2460)^-$ resonances are measured, as are the complex amplitudes and fit fractions for all components included in the amplitude model. The model obtained will be an integral part of a future determination of the angle γ of the Cabibbo-Kobayashi-Maskawa quark mixing matrix using $B^0 \rightarrow DK^+ \pi^-$ decays.

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I. INTRODUCTION

Dalitz plot (DP) analysis of $B^0 \rightarrow DK^+ \pi^-$ decays has been proposed as a way to measure the unitarity triangle angle γ [1,2]. The sensitivity to $\gamma \equiv \arg[-V_{ud}V_{ub}^*/(V_{cd}V_{cb}^*)]$, where V_{xy} are elements of the Cabibbo-Kobayashi-Maskawa (CKM) quark mixing matrix [3,4], originates from the interference of $\bar{b} \rightarrow \bar{c}u\bar{s}$ and $\bar{b} \rightarrow \bar{u}c\bar{s}$ amplitudes. Such interference occurs when the neutral D meson is reconstructed in a final state that is accessible to both \bar{D}^0 and D^0 decays and therefore corresponds to an admixture of the two states [5,6]. One of the largest components of the $B^0 \rightarrow DK^+ \pi^-$ final state is $B^0 \rightarrow DK^*(892)^0$, for which both $\bar{b} \rightarrow \bar{c}u\bar{s}$ and $\bar{b} \rightarrow \bar{u}c\bar{s}$ amplitudes are color suppressed, making them comparable in magnitude and potentially enhancing CP violation effects [7]. Decay diagrams for the quasi-two-body contributions from $B^0 \rightarrow DK^*(892)^0$ and $B^0 \rightarrow D_2^*(2460)^- K^+$ decays are shown in Fig. 1. Observables sensitive to γ have been measured by LHCb with a quasi-two-body approach [8], but a DP analysis is expected to be more sensitive because interference between resonances provides the possibility to resolve ambiguities in the determination of γ .

In order to determine γ with this method, it is necessary to have an amplitude model of the $B^0 \rightarrow \bar{D}^0 K^+ \pi^-$ decay that proceeds through the favored $\bar{b} \rightarrow \bar{c}u\bar{s}$ transition. This can be achieved by reconstructing the \bar{D}^0 meson through the $K^+ \pi^-$ decay; in this way the contribution from the $\bar{b} \rightarrow \bar{c}u\bar{s}$ amplitude is dominant and effects due to $\bar{b} \rightarrow \bar{u}c\bar{s}$ amplitudes can be neglected. While the analysis of this

decay chain is not itself sensitive to γ , its outcome will be an integral part of a future analysis using, for example, $D \rightarrow K^+ K^-$ decays where CP violation effects are expected as the final state is common to both D^0 and \bar{D}^0 decays.

Dalitz plot analyses of B meson decays to final states containing a charmed meson and two charged particles (either pions or kaons) also provide opportunities for studies of the spectroscopy of charmed mesons. Results in this area have recently been obtained from DP analyses of $B_s^0 \rightarrow \bar{D}^0 K^- \pi^+$ [9,10], $B^+ \rightarrow D^- K^+ \pi^+$ [11] and $B^0 \rightarrow \bar{D}^0 \pi^+ \pi^-$ [12] decays, all from LHCb. As the branching fraction for $B^0 \rightarrow \bar{D}^0 K^+ \pi^-$ decays is smaller than that for $B^0 \rightarrow \bar{D}^0 \pi^+ \pi^-$ decays, the analysis presented in this paper is not as sensitive to the parameters of charm resonances as that of Ref. [12]. However, the much larger sample of B mesons available at LHCb compared to that used in the only other published DP analysis of $B^0 \rightarrow \bar{D}^0 \pi^+ \pi^-$ decays from the Belle Collaboration [13] allows useful results on excited charm mesons to be obtained. Moreover, results on charm meson spectroscopy obtained from DP analysis of $B^0 \rightarrow \bar{D}^0 K^+ \pi^-$ decays provide important independent cross-checks of results from studies of the $B^0 \rightarrow \bar{D}^0 \pi^+ \pi^-$ DP, as possible biases due to other structures in the Dalitz plots are different between the two modes.

In this paper an amplitude analysis of the $B^0 \rightarrow \bar{D}^0 K^+ \pi^-$ decay is reported. The inclusion of charge-conjugate processes is implied throughout the paper. The analysis is based on a data sample corresponding to an integrated luminosity of 3.0 fb^{-1} of pp collision data collected with the LHCb detector in 2011 and 2012, when the collision center-of-mass energy was $\sqrt{s} = 7 \text{ TeV}$ (1.0 fb^{-1}) and $\sqrt{s} = 8 \text{ TeV}$ (2.0 fb^{-1}), respectively. Previously, the branching fraction for the three-body decay has been measured [14,15], and the $B^0 \rightarrow \bar{D}^0 K^*(892)^0$ [16,17]

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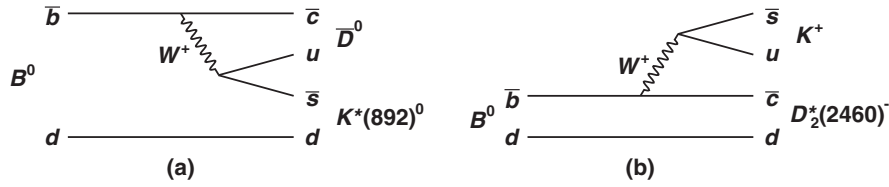


FIG. 1. Decay diagrams for the quasi-two-body contributions to $B^0 \rightarrow DK^+\pi^-$ from (a) $B^0 \rightarrow DK^*(892)^0$ and (b) $B^0 \rightarrow D_2^*(2460)^- K^+$ decays.

and $B^0 \rightarrow D_2^*(2460)^- K^+$ [14] contributions have been measured using quasi-two-body approaches; however this is the first DP analysis of the $B^0 \rightarrow \bar{D}^0 K^+ \pi^-$ decay.

The paper is organized as follows. A description of the LHCb detector, reconstruction and simulation software is given in Sec. II. The selection of signal candidates is described in Sec. III, and the determination of signal and background yields is presented in Sec. IV. An overview of the Dalitz plot analysis formalism is given in Sec. V, and details of the implementation of the amplitude analysis are presented in Sec. VI. The evaluation of systematic uncertainties is described in Sec. VII, with results and a brief summary given in Sec. VIII.

II. LHCb DETECTOR AND SOFTWARE

The LHCb detector [18,19] is a single-arm forward spectrometer covering the pseudorapidity range $2 < \eta < 5$, designed for the study of particles containing b or c quarks. The detector includes a high-precision tracking system consisting of a silicon-strip vertex detector [20] surrounding the pp interaction region, a large-area silicon-strip detector located upstream of a dipole magnet with a bending power of about 4 Tm, and three stations of silicon-strip detectors and straw drift tubes [21] placed downstream of the magnet. The polarity of the dipole magnet is reversed periodically throughout data taking. The tracking system provides a measurement of momentum, p , of charged particles with a relative uncertainty that varies from 0.5% at low momentum to 1.0% at 200 GeV (natural units with $c = \hbar = 1$ are used). The minimum distance of a track to a primary vertex, the impact parameter (IP), is measured with a resolution of $(15 + 29/p_T) \mu\text{m}$, where p_T is the component of the momentum transverse to the beam, in GeV. Different types of charged hadrons are distinguished using information from two ring-imaging Cherenkov detectors [22]. Photon, electron and hadron candidates are identified by a calorimeter system consisting of scintillating-pad and preshower detectors, an electromagnetic calorimeter and a hadronic calorimeter. Muons are identified by a system composed of alternating layers of iron and multiwire proportional chambers [23].

The trigger [24] consists of a hardware stage, based on information from the calorimeter and muon systems, followed by a software stage, in which all tracks with $p_T > 500(300)$ MeV are reconstructed for data collected in 2011

(2012). The software trigger used in this analysis requires a two-, three- or four-track secondary vertex with significant displacement from any primary pp interaction vertex (PV). At least one charged particle must have $p_T > 1.7$ GeV and be inconsistent with originating from a PV. A multivariate algorithm [25] is used for the identification of secondary vertices consistent with the decay of a b hadron.

In the off-line selection, the objects that prompted a positive trigger decision are associated with reconstructed particles. Selection requirements can therefore be made not only on whether the hardware trigger decision was due to a signature in the calorimeters or in the muon system, but on whether the decision was due to the signal candidate, other particles produced in the pp collision, or a combination of both. Signal candidates are accepted off-line if at least one of the final-state particles created a cluster in the hadronic calorimeter with sufficient transverse energy to fire the hardware trigger. Events that are triggered at the hardware level by another particle in the event are also retained. After all selection requirements are imposed, 67% of events in the sample were triggered by the decay products of the signal candidate, while the remainder were triggered only by another particle in the event.

Simulated events are used to characterize the detector response to signal and certain types of background events. In the simulation, pp collisions are generated using PYTHIA [26] with a specific LHCb configuration [27]. Decays of hadronic particles are described by EvtGen [28], in which final-state radiation is generated using Photos [29]. The interaction of the generated particles with the detector, and its response, are implemented using the Geant4 toolkit [30] as described in Ref. [31].

III. SELECTION REQUIREMENTS

The selection requirements follow closely those used in Ref. [10]. The more copious $B^0 \rightarrow \bar{D}^0 \pi^+ \pi^-$ decay is topologically and kinematically similar to the $B^0 \rightarrow \bar{D}^0 K^+ \pi^-$ channel, allowing it to be used as a control mode to optimize the selection requirements. Loose initial requirements are used to obtain a visible signal peak of $\bar{D}^0 \pi^+ \pi^-$ candidates. The tracks are required to be of good quality and must be above thresholds in p , p_T and χ_{IP}^2 , where χ_{IP}^2 is defined as the difference in χ^2 of a given PV reconstructed with and without the considered particle. The $\bar{D}^0 \rightarrow K^+ \pi^-$ candidate must satisfy criteria on its vertex

quality (χ^2_{vtx}) and flight distance from any PV and from the B candidate vertex, and must have invariant mass $m(K^+\pi^-)$ in the range 1814–1914 MeV. A requirement on the output of a boosted decision tree (BDT) that identifies $\bar{D}^0 \rightarrow K^+\pi^-$ decays originating from b hadron decays (\bar{D}^0 BDT) [32,33] is also applied. Candidate B mesons are selected with requirements on invariant mass, χ^2_{IP} and on the cosine of the angle between the B momentum vector and the line from the PV under consideration to the B vertex ($\cos\theta_{\text{dir}}$). A requirement is placed on the χ^2 of a kinematic fit [34] to the candidate's decay chain in which the \bar{D}^0 mass is constrained to its nominal value. The four final-state tracks must satisfy pion and kaon particle identification (PID) criteria.

A neural network [35] is used to discriminate between signal decays and combinatorial background. The *sPlot* technique [36], with the B candidate mass as the discriminating variable, is used to separate statistically $B^0 \rightarrow \bar{D}^0\pi^+\pi^-$ decays from background. The signal and background weights returned by this method are applied to the candidates, which are then used to train the network. The network is trained using 16 variables. They include the χ^2_{IP} of the four final-state tracks and the following variables associated to the \bar{D}^0 candidate: χ^2_{IP} , χ^2_{vtx} , the square of the flight distance from the PV divided by its uncertainty squared (χ^2_{flight}), $\cos\theta_{\text{dir}}$, and the output of the \bar{D}^0 BDT. In addition, the following variables associated to the B candidate are included: p_{T} , χ^2_{IP} , χ^2_{vtx} , χ^2_{flight} , and $\cos\theta_{\text{dir}}$. The p_{T} asymmetry [10] and track multiplicity in a cone with half-angle of 1.5 units of the plane of pseudorapidity and azimuthal angle (measured in radians) around the B candidate flight direction, which contain information about the isolation of the B candidate from the rest of the event, are also used. The input quantities to the neural network depend only weakly on the position of the candidate in the B decay Dalitz plot and therefore any requirement on the network output cannot appreciably bias the DP distribution. A requirement imposed on the network output reduces the combinatorial background remaining after the initial selection by a factor of 5 while retaining more than 90% of the signal.

The $B^0 \rightarrow \bar{D}^0 K^+\pi^-$ candidates must satisfy the same selection as the $B^0 \rightarrow \bar{D}^0\pi^+\pi^-$ decays, except for the PID requirement on the positively charged track from the B decay vertex, which is imposed to preferentially select kaons rather than pions. The PID efficiency is evaluated from calibration samples of $D^0 \rightarrow K^-\pi^+$ decays from the $D^{*+} \rightarrow D^0\pi^+$ decay chain. The kinematics of this decay chain can be exploited to obtain clean samples without using the PID information [22]. The PID efficiency of the requirements on the four tracks in the final state is around 50% and varies depending on the kinematics of the tracks, as described in detail in Sec. VI A.

Candidates are vetoed when the difference between $m(K^+\pi^-\pi^-)$ and $m(K^+\pi^-)$ lies within ± 2.5 MeV of the known $D^{*}(2010)^- - \bar{D}^0$ mass difference [37] to remove

background containing $D^{*-} \rightarrow \bar{D}^0\pi^-$ decays. Candidates are also rejected if a similar mass difference calculated with the pion mass hypothesis applied to the bachelor kaon satisfies the same criterion. To reject backgrounds from $B^0 \rightarrow D^-K^+$, $D^- \rightarrow K^+\pi^-\pi^-$ decays, it is required that the combination of the pion from the \bar{D}^0 candidate together with the two bachelor particles does not have an invariant mass in the range 1850–1890 MeV. Additionally, candidates are removed if the pion and kaon originating directly from the B^0 decay combine to give an invariant mass consistent with that of the D^0 meson (1835–1880 MeV). This removes candidates with the \bar{D}^0 wrongly reconstructed as well as potential background from $B^0 \rightarrow D^0\bar{D}^0$ decays. Other incorrectly reconstructed candidates are removed by vetoing candidates where the pion from the \bar{D}^0 decay and the kaon originating directly from the B^0 decay give an invariant mass in the range 1850–1885 MeV. At least one of the pion candidates is required to have no associated hits in the muon system to remove potential background from $B^0 \rightarrow J/\psi K^{*0}$ decays. Charmless decays of b hadrons are suppressed by the use of the \bar{D}^0 BDT and further reduced to a negligible level by requiring that the \bar{D}^0 candidate vertex is separated from the B^0 decay vertex by at least 1 mm.

Signal candidates are retained for further analysis if they have invariant mass in the range 5100–5900 MeV. After all selection requirements are applied, fewer than 1% of selected events also contain a second candidate. Such multiple candidates are retained and treated in the same manner as other candidates; the associated systematic uncertainty is negligible.

IV. DETERMINATION OF SIGNAL AND BACKGROUND YIELDS

The signal and background yields are determined from an extended maximum likelihood fit to the B candidate invariant mass distribution. The fit allows for signal decays, combinatorial background and contributions from other b hadron decays. The decay chain $B^0 \rightarrow \bar{D}^{*0}K^+\pi^-$ with $\bar{D}^{*0} \rightarrow \bar{D}^0\gamma$ or $\bar{D}^0\pi^0$ forms a partially reconstructed background that peaks at low B candidate mass as the neutral particle is not included in the candidate. Misidentified $B^0 \rightarrow \bar{D}^{(*)0}\pi^+\pi^-$, $\bar{\Lambda}_b^0 \rightarrow \bar{D}^{(*)0}K^+\bar{p}$ and $B_{(s)}^0 \rightarrow \bar{D}^{(*)0}K^+K^-$ decays are found to contribute to the background. A possible contribution from the highly suppressed $B_s^0 \rightarrow \bar{D}^0 K^+\pi^-$ decay mode is also included in the fit.

The signal peak is modeled with the sum of two Crystal Ball [38] functions, which have tails on opposite sides and which share a common mean. The tail parameters are fixed to the values found in fits to simulated signal decays. The relative normalization and the ratio of widths of the two functions are constrained, within uncertainties, to the values determined in a fit to $B^0 \rightarrow \bar{D}^0\pi^+\pi^-$ data. The

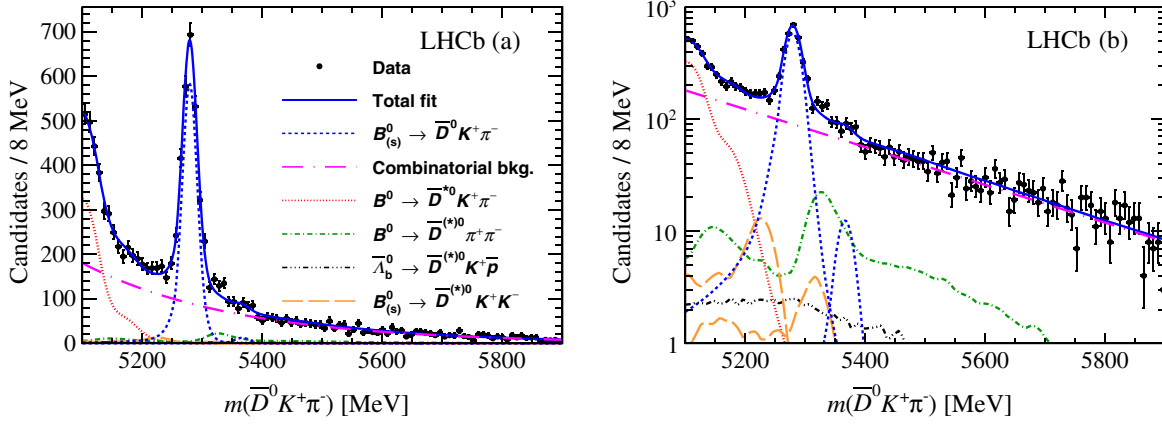


FIG. 2 (color online). Results of the fit to the B candidate invariant mass distribution with (a) linear and (b) logarithmic y-axis scales. The components are as described in the legend.

$B_s^0 \rightarrow \bar{D}^0 K^+ \pi^-$ shape is modeled identically to the signal peak, with the difference between the B^0 and B_s^0 mass peak positions fixed to its known value [37]. An exponential shape is used to model the combinatorial background.

Misidentified and partially reconstructed backgrounds are modeled with smoothed nonparametric functions. Simulated samples are used to obtain the shape for $B^0 \rightarrow \bar{D}^{*0} K^+ \pi^-$ decays, with the $\bar{D}^{*0} \rightarrow \bar{D}^0 \gamma$ and $\bar{D}^{*0} \pi^0$ contributions generated in the correct proportions [37]. To account for differences between simulation and data, for example in the polarization of the \bar{D}^{*0} meson, the B candidate invariant mass distribution for partially reconstructed $B^0 \rightarrow \bar{D}^{*0} K^+ \pi^-$ decays is allowed to be shifted by an offset that is a free parameter of the fit. The misidentified background shapes are also obtained from simulated samples. For $B^0 \rightarrow \bar{D}^{(*)0} \pi^+ \pi^-$ decays the \bar{D}^0 and \bar{D}^{*0} contributions are combined according to their relative branching fractions [37]. The backgrounds from $\bar{\Lambda}_b^0 \rightarrow \bar{D}^{(*)0} K^+ \bar{p}$ and $B_{(s)}^0 \rightarrow \bar{D}^{(*)0} K^+ K^-$ decays are assumed to have equal branching fractions for the decays with \bar{D}^0 and \bar{D}^{*0} mesons in the final state, as the decays involving \bar{D}^{*0} mesons have not yet been measured. The simulated samples are reweighted according to the relevant particle identification and misidentification probabilities and to match known DP distributions [12,39–41]. The (mis) identification probabilities take account of track kinematics and are calculated using calibration samples of $D^{*+} \rightarrow D^0 \pi^+$, $D^0 \rightarrow K^- \pi^+$ and $\Lambda \rightarrow p \pi^-$ decays [19,22]. The yields of the misidentified backgrounds relative to the signal are constrained, within uncertainties, to their expected values based on their known branching fractions [12,39,40] and misidentification probabilities.

There are 14 free parameters in the fit model: the mean and width of the signal shape, the relative normalization and relative width of the two Crystal Ball functions, the slope of the exponential function, the offset of the $B^0 \rightarrow \bar{D}^{*0} K^+ \pi^-$ shape and the yields of the eight contributions.

The result of the fit is shown in Fig. 2 and the yields are summarized in Table I. The yields are also reported within the signal region used in the Dalitz plot fit, corresponding to ± 2.5 widths of the B^0 signal shape (5248.55–5309.05 MeV). The distribution of candidates in the signal region over the Dalitz plot is shown in Fig. 3(a). Note that a B^0 mass constraint is applied to calculate the variables that are used to describe the Dalitz plot [42], improving the resolution of those variables and giving a unique kinematic boundary.

V. DALITZ PLOT ANALYSIS FORMALISM

In $B^0 \rightarrow \bar{D}^0 K^+ \pi^-$ decays, resonances are expected in the $m^2(\bar{D}^0 \pi^-)$ and $m^2(K^+ \pi^-)$ combinations, so the Dalitz plot shown in Fig. 3(a) is defined in terms of these two invariant mass squared terms. For a fixed B^0 mass, these two invariant mass squared combinations can be used to calculate all other relevant kinematic quantities.

The isobar model [43–45] is used to describe the complex decay amplitude. The total amplitude is given by the coherent sum of amplitudes from resonant and nonresonant intermediate contributions and is given by

TABLE I. Yields from the fit to the $\bar{D}^0 K^+ \pi^-$ data sample. The full mass range is 5100–5900 MeV and the signal region is 5248.55–5309.05 MeV.

Component	Full mass range	Signal region
$B^0 \rightarrow \bar{D}^0 K^+ \pi^-$	2576 ± 72	2344 ± 66
$B_s^0 \rightarrow \bar{D}^0 K^+ \pi^-$	55 ± 27	1 ± 1
Combinatorial background	5540 ± 187	684 ± 23
$B^0 \rightarrow \bar{D}^{*0} K^+ \pi^-$	1750 ± 99	6 ± 1
$B^0 \rightarrow \bar{D}^{(*)0} \pi^+ \pi^-$	485 ± 47	51 ± 5
$\bar{\Lambda}_b^0 \rightarrow \bar{D}^{(*)0} K^+ \bar{p}$	95 ± 26	18 ± 5
$B^0 \rightarrow \bar{D}^{(*)0} K^+ K^-$	127 ± 27	10 ± 2
$B_s^0 \rightarrow \bar{D}^{(*)0} K^+ K^-$	54 ± 18	14 ± 5

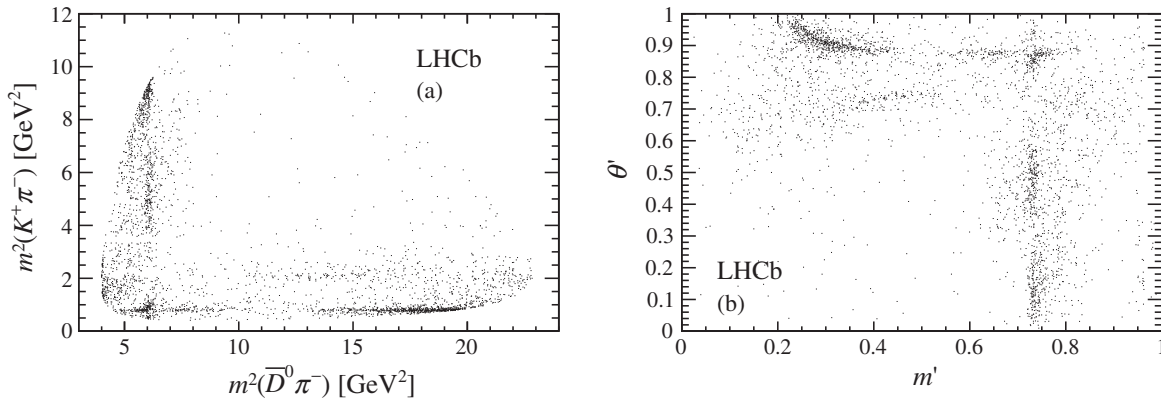


FIG. 3. Distribution of $B^0 \rightarrow \bar{D}^0 K^+ \pi^-$ candidates in the signal region over (a) the Dalitz plot and (b) the square Dalitz plot. The definition of the square Dalitz plot is given in Sec. VI A.

$$\begin{aligned} \mathcal{A}(m^2(\bar{D}^0 \pi^-), m^2(K^+ \pi^-)) \\ = \sum_{j=1}^N c_j F_j(m^2(\bar{D}^0 \pi^-), m^2(K^+ \pi^-)), \end{aligned} \quad (1)$$

where c_j are complex coefficients describing the relative contribution for each intermediate process. The resonant dynamics are contained in the $F_j(m^2(\bar{D}^0 \pi^-), m^2(K^+ \pi^-))$ terms that are normalized such that the integral of the squared magnitude over the DP is unity for each term. For a $\bar{D}^0 \pi^-$ resonance $F_j(m^2(\bar{D}^0 \pi^-), m^2(K^+ \pi^-))$ is given by

$$\begin{aligned} F(m^2(\bar{D}^0 \pi^-), m^2(K^+ \pi^-)) \\ = R(m(\bar{D}^0 \pi^-)) \times X(|\vec{p}|r_{\text{BW}}) \times X(|\vec{q}|r_{\text{BW}}) \times T(\vec{p}, \vec{q}), \end{aligned} \quad (2)$$

where \vec{p} is the bachelor particle momentum and \vec{q} is the momentum of one of the resonance daughters, both evaluated in the $\bar{D}^0 \pi^-$ rest frame. The functions R , X and T are described below.

The $X(z)$ terms are Blatt-Weisskopf barrier factors [46], where $z = |\vec{q}|r_{\text{BW}}$ or $|\vec{p}|r_{\text{BW}}$ and r_{BW} is the barrier radius which is set to $4.0 \text{ GeV}^{-1} \approx 0.8 \text{ fm}$ [10] for all resonances. The barrier factors are angular momentum dependent and are given by

$$\begin{aligned} L=0: X(z) &= 1, \quad L=1: X(z) = \sqrt{\frac{1+z_0^2}{1+z^2}}, \\ L=2: X(z) &= \sqrt{\frac{z_0^4 + 3z_0^2 + 9}{z^4 + 3z^2 + 9}}, \\ L=3: X(z) &= \sqrt{\frac{z_0^6 + 6z_0^4 + 45z_0^2 + 225}{z^6 + 6z^4 + 45z^2 + 225}}, \end{aligned} \quad (3)$$

where z_0 is the value of z at the pole mass of the resonance and L is the orbital angular momentum between the

resonance and the bachelor particle. Since the parent and daughter particles all have zero spin, L is also the spin of the resonance.

The $T(\vec{p}, \vec{q})$ terms describe the angular distributions in the Zemach tensor formalism [47,48] and are given by

$$\begin{aligned} L=0: T(\vec{p}, \vec{q}) &= 1, \\ L=1: T(\vec{p}, \vec{q}) &= -2\vec{p} \cdot \vec{q}, \\ L=2: T(\vec{p}, \vec{q}) &= \frac{4}{3}[3(\vec{p} \cdot \vec{q})^2 - (|\vec{p}||\vec{q}|)^2], \\ L=3: T(\vec{p}, \vec{q}) &= -\frac{24}{15}[5(\vec{p} \cdot \vec{q})^3 - 3(\vec{p} \cdot \vec{q})(|\vec{p}||\vec{q}|)^2]. \end{aligned} \quad (4)$$

These expressions are proportional to the Legendre polynomials, $P_L(x)$, where x is the cosine of the angle between \vec{p} and \vec{q} (referred to as the helicity angle).

The $R(m(\bar{D}^0 \pi^-))$ functions are the mass line shapes. Resonant contributions are typically described by the relativistic Breit-Wigner (RBW) function

$$R(m) = \frac{1}{(m_0^2 - m^2) - im_0\Gamma(m)}, \quad (5)$$

where the mass-dependent decay width is

$$\Gamma(m) = \Gamma_0 \left(\frac{q}{q_0} \right)^{2L+1} \left(\frac{m_0}{m} \right) X^2(qr_{\text{BW}}), \quad (6)$$

where q_0 is the value of $q = |\vec{q}|$ when the invariant mass is equal to the pole mass of the resonance, m_0 .

The large phase space available in B decays allows for the presence of nonresonant amplitudes (i.e. contributions that do not proceed via a known resonance) that vary across the Dalitz plot. An exponential form factor (EFF) has been found to describe nonresonant contributions well in several DP analyses of B decays [49],

$$R(m) = \exp[-\alpha m^2], \quad (7)$$

where α is a shape parameter that must be determined from the data and m is a two-body invariant mass [$m(\bar{D}^0\pi^-)$ in this example].

The RBW function is a good model for narrow resonances that are well separated from any other resonant or nonresonant contribution of the same spin. This approach is known to break down in the $K\pi$ S-wave because the $\bar{K}_0^*(1430)$ resonance interferes strongly with a slowly varying nonresonant term, as described in Ref. [50]. The LASS line shape [51] has been developed to combine these two contributions,

$$R(m) = \frac{m}{q \cot \delta_B - iq} + \exp[2i\delta_B] \frac{m_0 \Gamma_0 \frac{m_0}{q_0}}{(m_0^2 - m^2) - im_0 \Gamma_0 \frac{q}{m q_0}}, \quad (8)$$

$$\text{where } \cot \delta_B = \frac{1}{aq} + \frac{1}{2}rq, \quad (9)$$

and where m_0 and Γ_0 are the pole mass and width of the $\bar{K}_0^*(1430)$ state, and a and r are shape parameters.

The $D\pi$ S-wave nonresonant contribution can be described by the “dabba” line shape [52], defined as

$$R(m) = \frac{B'(m^2)(m^2 - s_A)\rho}{1 - \beta(m^2 - m_{\min}^2) - iB'(m^2)(m^2 - s_A)\rho}, \quad (10)$$

where

$$B'(m^2) = b \exp[-\alpha(m^2 - m_{\min}^2)]. \quad (11)$$

Here m_{\min} is the invariant mass at threshold, $s_A = m_D^2 - 0.5m_\pi^2$ is the Adler zero, ρ is a phase-space factor and b , α and β are parameters with values fixed to 24.49 GeV^{-2} , 0.1 GeV^{-2} and 0.1 GeV^{-2} , respectively, according to Ref. [52].

Ignoring reconstruction and selection effects, the DP probability density function would be

$$\mathcal{P}_{\text{phys}}(m^2(\bar{D}^0\pi^-), m^2(K^+\pi^-)) = \frac{|\mathcal{A}(m^2(\bar{D}^0\pi^-), m^2(K^+\pi^-))|^2}{\int \int_{\text{DP}} |\mathcal{A}|^2 dm^2(\bar{D}^0\pi^-) dm^2(K^+\pi^-)}, \quad (12)$$

where the dependence of \mathcal{A} on the DP position has been suppressed in the denominator for brevity. The primary results of most Dalitz plot analyses are the complex coefficients, as defined in Eq. (1). These, however, depend on the choice of phase convention, amplitude formalism and normalization used in each analysis. The convention-independent quantities of fit fractions and interference fit fractions provide a way to reliably compare results between different analyses. Fit fractions are defined as the integral of the amplitude for each intermediate component squared, divided by that of the coherent matrix element squared for all intermediate contributions,

$$FF_j = \frac{\int \int_{\text{DP}} |c_j F_j(m^2(\bar{D}^0\pi^-), m^2(K^+\pi^-))|^2 dm^2(\bar{D}^0\pi^-) dm^2(K^+\pi^-)}{\int \int_{\text{DP}} |\mathcal{A}|^2 dm^2(\bar{D}^0\pi^-) dm^2(K^+\pi^-)}. \quad (13)$$

The fit fractions need not sum to unity due to possible net constructive or destructive interference, described by interference fit fractions defined (for $i < j$ only) by

$$FF_{ij} = \frac{\int \int_{\text{DP}} 2\text{Re}[c_i c_j^* F_i F_j^*] dm^2(\bar{D}^0\pi^-) dm^2(K^+\pi^-)}{\int \int_{\text{DP}} |\mathcal{A}|^2 dm^2(\bar{D}^0\pi^-) dm^2(K^+\pi^-)}, \quad (14)$$

where the dependence of $F_i^{(*)}$ and \mathcal{A} on the DP position has been omitted.

VI. DALITZ PLOT FIT

A. Signal efficiency

The variation of the efficiency across the phase space is studied in terms of the square Dalitz plot (SDP). The SDP is defined by variables m' and θ' that range between 0 and 1 and are given for the $\bar{D}^0 K^+ \pi^-$ case by

$$m' \equiv \frac{1}{\pi} \arccos \left(2 \frac{m(\bar{D}^0\pi^-) - m_{\bar{D}^0\pi^-}^{\min}}{m_{\bar{D}^0\pi^-}^{\max} - m_{\bar{D}^0\pi^-}^{\min}} - 1 \right) \quad \text{and} \quad \theta' \equiv \frac{1}{\pi} \theta(\bar{D}^0\pi^-), \quad (15)$$

where $m_{\bar{D}^0\pi^-}^{\max} = m_{B^0} - m_{K^+}$ and $m_{\bar{D}^0\pi^-}^{\min} = m_{\bar{D}^0} + m_{\pi^-}$ are the kinematic boundaries of $m(\bar{D}^0\pi^-)$ allowed in the $B^0 \rightarrow \bar{D}^0 K^+ \pi^-$ decay and $\theta(\bar{D}^0\pi^-)$ is the helicity angle of the $\bar{D}^0\pi^-$ system (the angle between the K^+ and the \bar{D}^0 meson in the $\bar{D}^0\pi^-$ rest frame). The distribution of selected events across the SDP is shown in Fig. 3(b).

Efficiency variation across the SDP is caused by the detector acceptance and by trigger, selection and PID requirements. The efficiency is evaluated with simulated samples generated uniformly over the SDP. Data-driven corrections are applied to correct for known differences between data and simulation in the tracking, trigger and PID efficiencies, using identical methods to those described

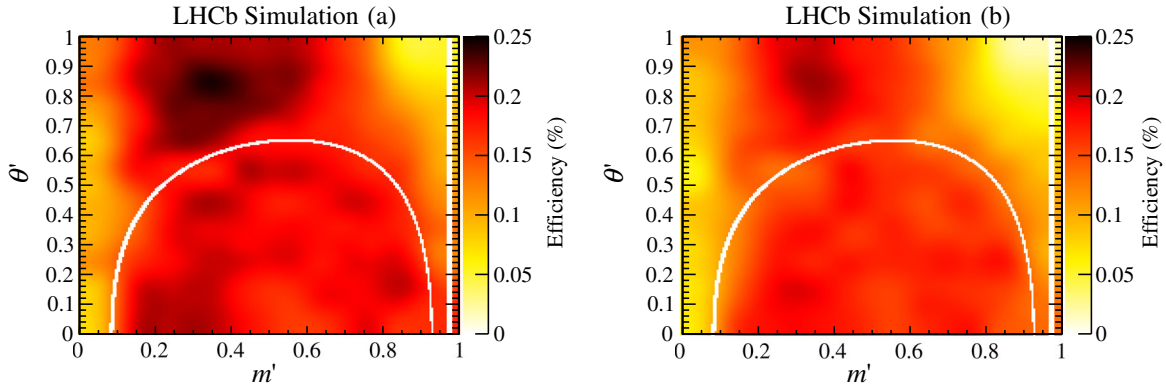


FIG. 4 (color online). Efficiency variation as a function of SDP position for candidates triggered by (a) signal decay products and (b) by the rest of the event. The vertical white stripe is due to the D^* veto and the curved white band is due to the \bar{D}^0 veto.

in Ref. [10]. The efficiency functions are obtained by fitting the corrected simulation with two-dimensional cubic splines. Figure 4 shows the histograms used to model the variation of the efficiency over the SDP for candidates triggered by (a) signal decays and (b) by the rest of the event.

B. Background studies

Among the background yields in the signal region, given in Table I, the only sizeable components are due to combinatorial background and $B^0 \rightarrow \bar{D}^{(*)0}\pi^+\pi^-$ decays. The SDP distributions of these backgrounds are described by the histograms shown in Fig. 5.

Combinatorial background contributes 22% of candidates in the signal region. The shape of this contribution over the SDP is obtained from the high B mass sideband (5400–5900 MeV). As seen in Fig. 2, this sideband is dominated by combinatorial background, with a small contribution from $B^0 \rightarrow \bar{D}^{(*)0}\pi^+\pi^-$ decays. The SDP distribution of the $B^0 \rightarrow \bar{D}^{(*)0}\pi^+\pi^-$ contribution in the sideband region is modeled as described below for the signal region and is subtracted from the sideband sample. To

check that the SDP shape of the combinatorial background does not vary with the B candidate mass, a sample of doubly charged $\bar{D}^0 K^\pm \pi^\pm$ candidates is investigated. This confirms that the SDP distribution from the sideband is a reliable model for combinatorial background in the signal region.

The $B^0 \rightarrow \bar{D}^{(*)0}\pi^+\pi^-$ contribution accounts for 1.6% of the candidates in the signal region. Its SDP distribution is obtained from a simulated sample, with the $B^0 \rightarrow \bar{D}^0\pi^+\pi^-$ and $B^0 \rightarrow \bar{D}^{*0}\pi^+\pi^-$ contributions combined and reweighted as described in Sec. IV. The $B^0 \rightarrow \bar{D}^0\pi^+\pi^-$ decay mode is the dominant component of this background in the signal region.

Due to resolution effects, $B^0 \rightarrow D^*(2010)^- K^+$, $D^*(2010)^- \rightarrow \bar{D}^0\pi^-$ decays are not entirely removed by the D^* veto. Although this component corresponds to real $B^0 \rightarrow \bar{D}^0\pi^- K^+$ decays, it is treated as incoherent (i.e. as background) since its interference with the remainder of the signal is negligible. Its SDP distribution is modeled as a Gaussian peak in $m(\bar{D}^0\pi^-)$, with mean fixed to the known $D^*(2010)^-$ mass and width and yield determined in the fit to data.

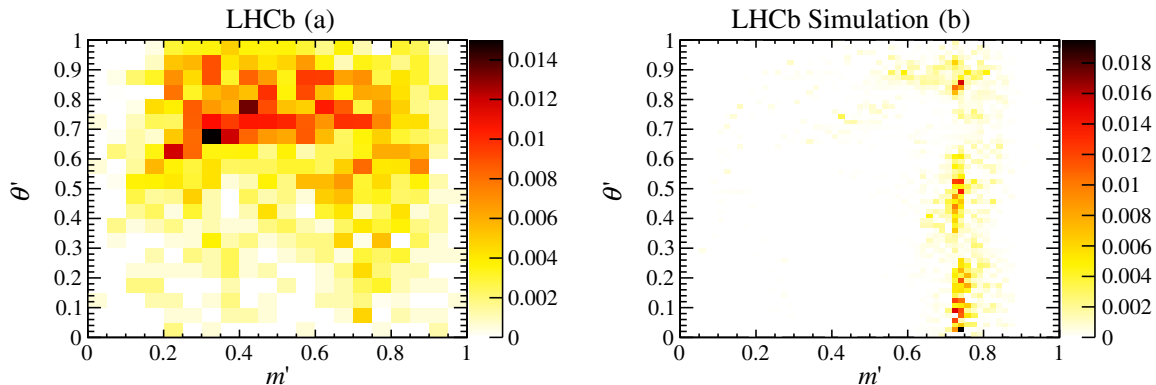


FIG. 5 (color online). SDP distributions of the background contributions from (a) combinatorial background and (b) $B^0 \rightarrow \bar{D}^{(*)0}\pi^+\pi^-$ decays.

TABLE II. Signal contributions to the fit model, where parameters and uncertainties are taken from Ref. [37]. The models are described in Sec. V.

Resonance	Spin	DP axis	Model	Parameters
$K^*(892)^0$	1	$m^2(K^+\pi^-)$	RBW	$m_0 = 895.81 \pm 0.19$ MeV, $\Gamma_0 = 47.4 \pm 0.6$ MeV
$K^*(1410)^0$	1	$m^2(K^+\pi^-)$	RBW	$m_0 = 1414 \pm 15$ MeV, $\Gamma_0 = 232 \pm 21$ MeV
$K_0^*(1430)^0$	0	$m^2(K^+\pi^-)$	LASS	Determined from data (see text)
$K_2^*(1430)^0$	2	$m^2(K^+\pi^-)$	RBW	$m_0 = 1432.4 \pm 1.3$ MeV, $\Gamma_0 = 109 \pm 5$ MeV
$D_0^*(2400)^-$	0	$m^2(\bar{D}^0\pi^-)$	RBW	Determined from data (see Table III)
$D_2^*(2460)^-$	2	$m^2(\bar{D}^0\pi^-)$	RBW	
Nonresonant	0	$m^2(\bar{D}^0\pi^-)$	dabba	Fixed (see text)
Nonresonant	1	$m^2(\bar{D}^0\pi^-)$	EFF	Determined from data (see text)

TABLE III. Masses and widths (MeV) determined in the fit to data, with statistical uncertainties only.

Resonance	Mass	Width
$D_0^*(2400)^-$	2360 ± 15	255 ± 26
$D_2^*(2460)^-$	2465.6 ± 1.8	46.0 ± 3.4

C. Amplitude model for $B^0 \rightarrow \bar{D}^0 K^+ \pi^-$ decays

The Dalitz plot fit is performed using the Laura++ [53] package. The likelihood function is given by

$$\mathcal{L} = \prod_i^{N_c} \left[\sum_k N_k \mathcal{P}_k(m_i^2(\bar{D}^0\pi^-), m_i^2(K^+\pi^-)) \right], \quad (16)$$

where the index i runs over N_c candidates, k runs over the signal and background components and N_k is the yield in each component. The probability density function for the signal component, \mathcal{P}_{sig} , is given by Eq. (12) with the $|\mathcal{A}(m^2(\bar{D}^0\pi^-), m^2(K^+\pi^-))|^2$ terms multiplied by the efficiency function described in Sec. VI A. As it is possible for the minimization procedure to find a local minimum of the negative log likelihood (NLL) profile, the fit is repeated

many times with randomized initial values to ensure the global minimum is found.

The nominal Dalitz plot fit model for $B^0 \rightarrow \bar{D}^0 K^+ \pi^-$ decays is composed of several resonant and nonresonant amplitudes. Only those amplitudes that provide significant contributions or that aid the fit stability are included. Unnatural spin-parity states are not considered as these do not decay to two pseudoscalars. The eight amplitudes included in this model are listed in Table II. The width of the narrowest signal contribution to the Dalitz plot (~ 50 MeV) is far larger than the mass resolution (~ 2.4 MeV); therefore, resolution effects are neglected.

The real and imaginary parts of the complex coefficients c_j defined in Eq. (1) are free parameters of the fit except for the coefficient of the $D_2^*(2460)^-$ component, which is fixed to 1 as a reference. The phases and magnitudes of the complex coefficients, as well as fit fractions and interference fit fractions are derived from these free parameters. In addition, the masses and widths of the $D_0^*(2400)^-$ and $D_2^*(2460)^-$ resonances are determined from the fit to data and are reported in Table III. The statistical uncertainties on all parameters of interest are calculated using large samples of simulated pseudoexperiments. These pseudoexperiments are also used to determine the correlations between the

TABLE IV. Complex coefficients and fit fractions determined from the Dalitz plot fit. Uncertainties are statistical only. Note that the fit fractions, magnitudes and phases are derived quantities.

Resonance	Fit fraction (%)	Isobar model coefficients			
		Real part	Imaginary part	Magnitude	Phase
$K^*(892)^0$	37.4 ± 1.5	-0.00 ± 0.15	-1.27 ± 0.06	1.27 ± 0.06	-1.57 ± 0.11
$K^*(1410)^0$	0.7 ± 0.3	0.15 ± 0.06	-0.09 ± 0.09	0.18 ± 0.07	-0.54 ± 0.21
$K_0^*(1430)^0$	5.1 ± 2.0	0.14 ± 0.38	0.45 ± 0.15	0.47 ± 0.09	1.27 ± 0.95
LASS nonresonant	4.8 ± 3.8	-0.10 ± 0.24	0.44 ± 0.14	0.46 ± 0.14	1.79 ± 0.65
LASS total	6.7 ± 2.7				
$K_2^*(1430)^0$	7.4 ± 1.7	-0.32 ± 0.09	-0.47 ± 0.07	0.57 ± 0.05	-2.16 ± 0.19
$D_0^*(2400)^-$	19.3 ± 2.8	-0.80 ± 0.08	-0.44 ± 0.14	0.91 ± 0.07	-2.64 ± 0.15
$D_2^*(2460)^-$	23.1 ± 1.2	1.00	0.00	1.00	0.00
$D\pi$ S-wave (dabba)	6.6 ± 1.4	-0.39 ± 0.09	0.36 ± 0.17	0.53 ± 0.07	2.40 ± 0.27
$D\pi$ P-wave (EFF)	8.9 ± 1.6	-0.62 ± 0.06	-0.03 ± 0.06	0.62 ± 0.06	-3.09 ± 0.10
Total fit fraction	113.4				

statistical uncertainties on the parameters, which are given in Appendix A. The LASS parameters are determined to be $m_0 = 1450 \pm 80$ MeV, $\Gamma_0 = 400 \pm 230$ MeV, $a = 3.2 \pm 1.8$ GeV and $r = 0.9 \pm 1.1$ GeV, while the parameter of the EFF line shape of the $D\pi$ P-wave nonresonant amplitude is determined to be $\alpha = 0.88 \pm 0.10$ GeV⁻².

The values of the fit fractions and complex coefficients obtained from the fit are shown in Table IV, while the values of the interference fit fractions are given in Appendix B. The sum of the fit fractions is seen to exceed unity, mostly due to interference within the $D\pi$ and $K\pi$ S-waves. Note that in Table IV, and all results for fit

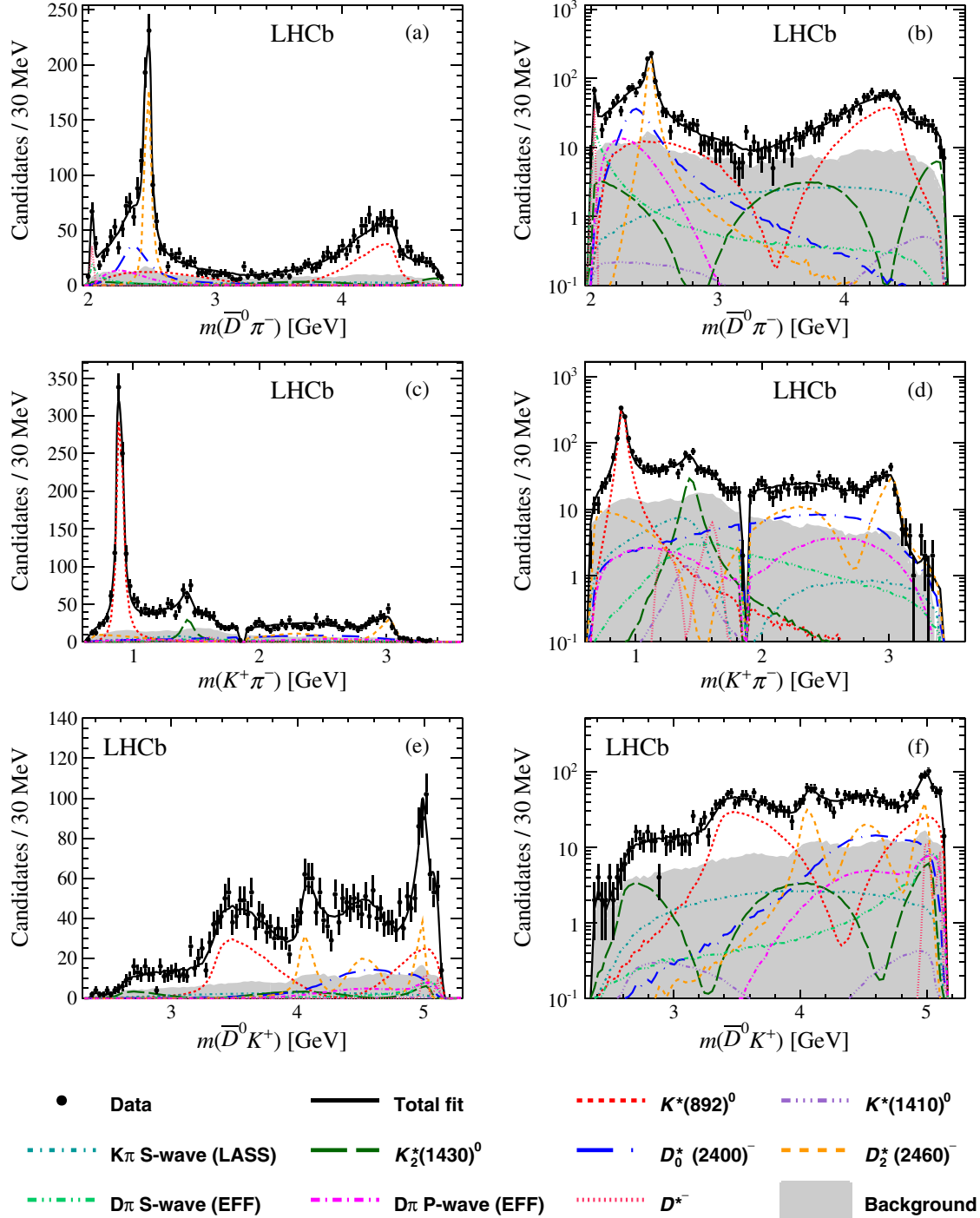


FIG. 6 (color online). Projections of the data and amplitude fit results onto (a) $m(\bar{D}^0\pi^-)$, (c) $m(K^+\pi^-)$ and (e) $m(\bar{D}^0K^+)$, with the same projections shown in (b), (d) and (f) with a logarithmic y-axis scale. Components are described in the legend.

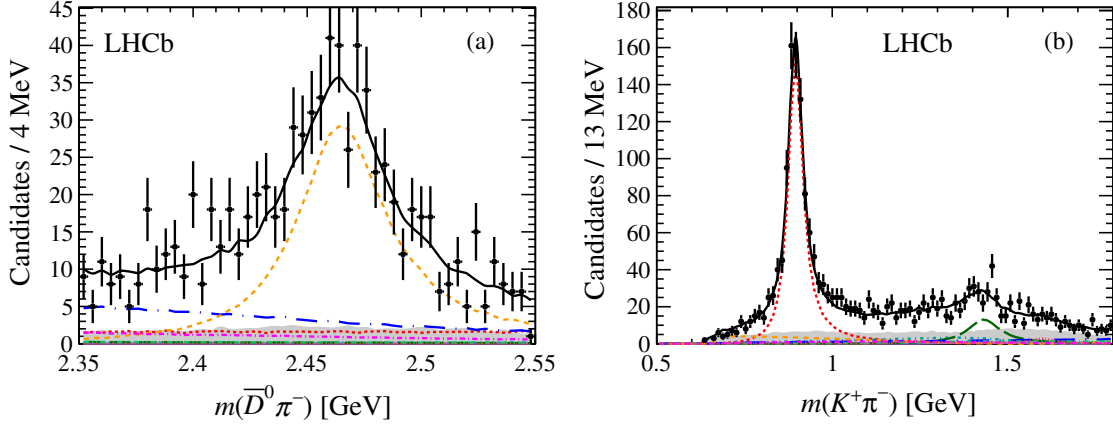


FIG. 7 (color online). Projections of the data and amplitude fit results onto (a) $m(\bar{D}^0 \pi^-)$ in the $D_2^*(2460)^-$ region and (b) the low $m(K^+ \pi^-)$ region. Components are as shown in Fig. 6.

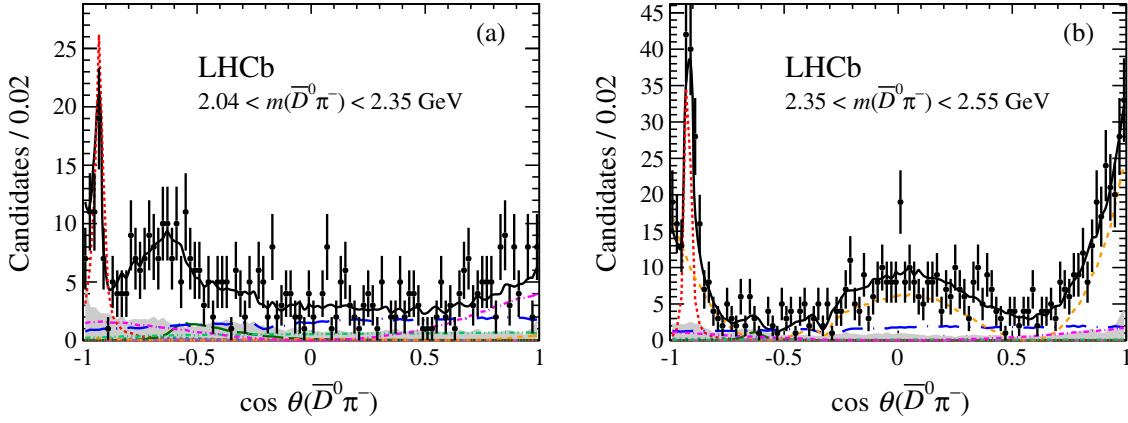


FIG. 8 (color online). Projections of the data and amplitude fit results onto $\cos \theta(\bar{D}^0 \pi^-)$ in the mass ranges (a) $2.04 < m(\bar{D}^0 \pi^-) < 2.35$ GeV and (b) $2.35 < m(\bar{D}^0 \pi^-) < 2.55$ GeV. Components are as shown in Fig. 6.

fractions and derived quantities, values are reported separately for both the $K_0^*(1430)^0$ and nonresonant components of the LASS line shape, as well as their coherent sum.

Projections of the data and the nominal fit model onto $m(K^+ \pi^-)$, $m(\bar{D}^0 \pi^-)$ and $m(\bar{D}^0 K^+)$ are shown in Fig. 6. Zooms are provided in the regions of the main resonant contributions in Fig. 7. Projections onto the cosine of the helicity angle of the $\bar{D}^0 \pi^-$ and $K^+ \pi^-$ systems are shown in Figs. 8 and 9, respectively. These projections all show good agreement between data and the fit model.

Angular moments provide a useful method to investigate the helicity structure of the decays. The angular moments in $m(\bar{D}^0 \pi^-)$ and $m(K^+ \pi^-)$, obtained as in Refs. [10,11], are shown in Figs. 10 and 11, respectively. The contributions due to the $K^*(892)^0$ and $D_2^*(2460)^-$ resonances are seen as peaks in moments up to order 2 and order 4, respectively, as expected for spin-1 and spin-2 resonances. Reflections make the interpretation of moments at higher masses more difficult. However, the good agreement seen between data

and the fit model provides further support for the fit model being a good description of the data.

The quality of the fit is evaluated by determining a two-dimensional χ^2 value, comparing the data and fit model in 144 bins across the SDP that are defined adaptively to ensure they are approximately equally populated. The pull in each of these bins, defined as the difference between the data and the fit model divided by the uncertainty, is shown in Fig. 12. The effective number of degrees of freedom of the χ^2 is between $N_{\text{bins}} - N_{\text{pars}} - 1$ and $N_{\text{bins}} - 1$, where N_{pars} is the number of free parameters in the fit, yielding a reduced χ^2 in the range 0.99–1.22. Additional unbinned tests of fit quality [54] also show acceptable agreement between the data and the fit model.

VII. SYSTEMATIC UNCERTAINTIES

Systematic uncertainties are considered from sources that can be divided into two categories, experimental and

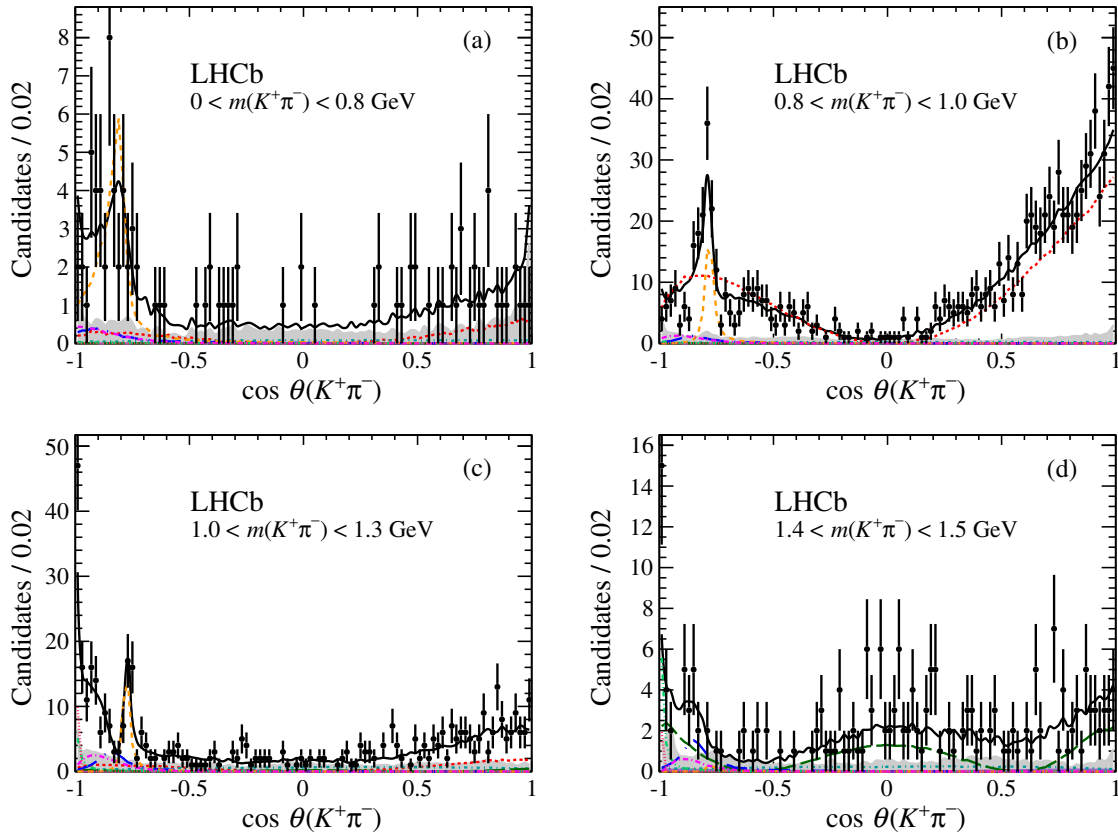


FIG. 9 (color online). Projections of the data and amplitude fit results onto $\cos \theta(K^+\pi^-)$ in the mass ranges (a) $m(K^+\pi^-) < 0.8$ GeV, (b) $0.8 < m(K^+\pi^-) < 1.0$ GeV, (c) $1.0 < m(K^+\pi^-) < 1.3$ GeV and (d) $1.4 < m(K^+\pi^-) < 1.5$ GeV. Components are as shown in Fig. 6.

model uncertainties. Experimental uncertainties arise due to the signal and background yields in the signal region, the distributions of the background components across the SDP, the variation of efficiency across the SDP, and possible bias due to the fitting procedure. Model uncertainties are considered due to the fixed parameters in the signal model, the addition or removal of marginal amplitudes, and the choice of models for the $K\pi$ S-wave and the $D\pi$ S- and P-waves. The uncertainties due to all of these sources are combined in quadrature.

The signal and background yields are determined from the fit to the B candidate invariant mass distribution. Systematic uncertainties are considered on the total yields due to both statistical and systematic variations of these yields, as evaluated in Ref. [15]. The yields in the signal region are varied appropriately and the effects of these variations on the parameters of interest are assigned as systematic uncertainties.

The histograms describing the background distributions are each varied within statistical uncertainties to establish the uncertainty due to the imperfect knowledge of the distribution of these backgrounds across the SDP. The histograms describing the efficiency variation across the SDP are also varied within their uncertainties prior to

the spline fit. The efficiency histograms are also varied with local correlations to account for the effects of any unknown correlations between neighboring bins. For each parameter the larger uncertainty is considered from the correlated and uncorrelated variations. In addition, the binning scheme of the control sample used to evaluate PID performance is varied.

An ensemble of pseudoexperiments is used to establish systematic uncertainties related to any potential fit bias. Pseudoexperiments are generated using the parameters determined in the fit to data, and mean fitted values of the parameters are determined from Gaussian fits to the distributions of results obtained in the ensemble. The differences between the generated and mean fitted values are found to be small. Uncertainties are determined as the sum in quadrature of the difference between the generated and mean fitted values, and the uncertainty on the mean fitted value from the Gaussian fit.

Systematic uncertainties due to fixed parameters in the fit model are determined by repeating the fit with these parameters varied. The fixed masses and widths are varied within their uncertainties as shown in Table II, while the Blatt-Weisskopf barrier radii, r_{BW} , are varied independently for $\bar{D}^0\pi^-$ and $K^+\pi^-$ resonances between 3 and 5 GeV^{-1} [10].

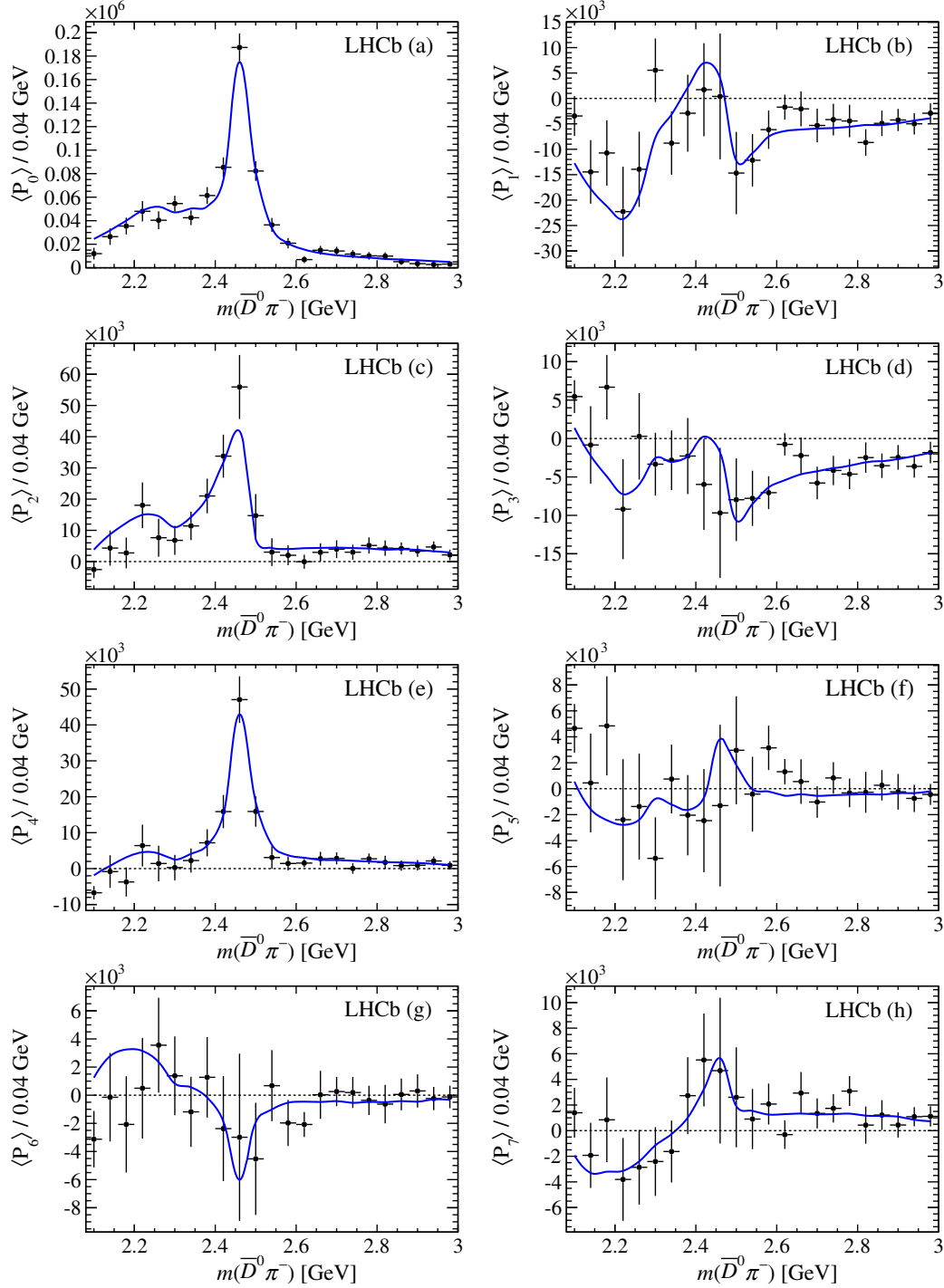


FIG. 10 (color online). Background-subtracted and efficiency-corrected Legendre moments up to order 7 calculated as a function of $m(\bar{D}^0 \pi^-)$ for data (black data points) and the fit result (solid blue curve).

The $K^*(1410)^0$ amplitude does not contribute significantly to the nominal fit model so the fit is repeated with this component removed and the change in results is assigned as the associated systematic uncertainty. In addition, uncertainties are assigned from the changes in the results when an amplitude due to the $K^*(1680)^0$

resonance or from a virtual $B^*(5325)^+$ component, as described in Ref. [10], is included in the model.

A Dalitz plot analysis of $B_s^0 \rightarrow \bar{D}^0 K^- \pi^+$ observed both spin-1 and spin-3 resonances at $m(\bar{D}^0 K^-) \sim 2.86 \text{ GeV}$ [9,10]. A spin-3 resonance has also been seen at $m(\bar{D}^0 \pi^-) \sim 2.76 \text{ GeV}$ in $B^0 \rightarrow \bar{D}^0 \pi^+ \pi^-$ decays [12], while

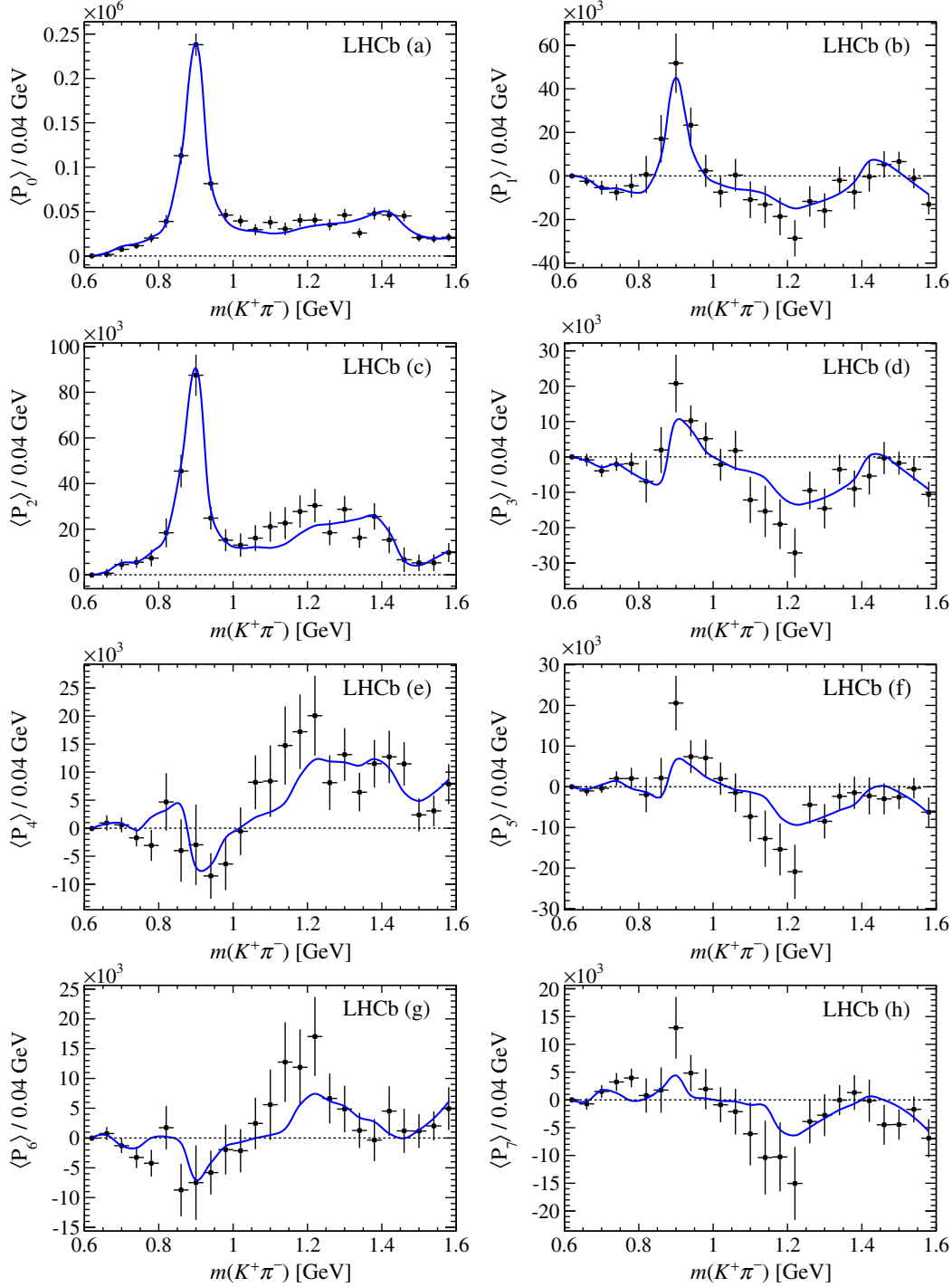


FIG. 11 (color online). Background-subtracted and efficiency-corrected Legendre moments up to order 7 calculated as a function of $m(K^+\pi^-)$ for data (black data points) and the fit result (solid blue curve).

an analysis of $B^+ \rightarrow D^- K^+ \pi^+$ shows a spin-1 resonance at similar $m(D^+\pi^-)$ values [11]. Uncertainties are assigned corresponding to the changes in results when either a spin-1 or spin-3 state at $m(\bar{D}^0\pi^-) \sim 2.76$ GeV is added to the nominal model.

The LASS model used to describe the $K\pi$ S-wave is replaced with a Flatté shape [55], which accounts for the

$K\eta'$ threshold near the $K_0^*(1430)^0$ mass, and a resonant term with a modified mass-dependent width [52] for the κ [also known as $K_0^*(800)$] state. This model gives an NLL that is worse by 4.4 units. A model-independent description of the $K\pi$ S-wave is also used to fit the data, with the uncertainty on each parameter taken as the larger of the two differences. This alternative improves the NLL by 8.8 units

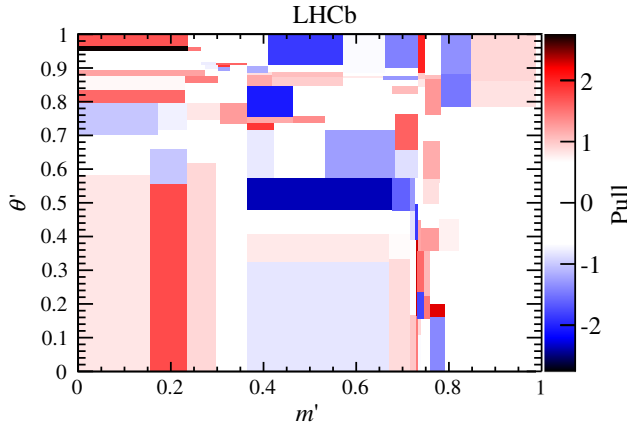


FIG. 12 (color online). Differences between the data SDP distribution and the fit model across the SDP, in terms of the per-bin pull.

but introduces an additional four free parameters into the fit. The dabba line shape used to describe the $\bar{D}^0\pi^-$ S-wave is replaced with an EFF line shape, while a power-law model is introduced as an alternative to the EFF line shape that describes the $\bar{D}^0\pi^-$ P-wave. These alterations worsen the NLL by 3.0 units and improve it by 0.8 units respectively.

The total systematic uncertainties due to experimental and model effects for fit fractions and complex coefficients are given together with the results in Sec. VIII. The contributions from different sources to the systematic uncertainties on the fit fractions, masses and widths are given in Tables V and VI. The dominant experimental systematic uncertainty on most parameters is due to either the efficiency variation or background distributions across the SDP, while the model uncertainties are generally dominated by the effects of alternative descriptions of

the $K\pi$ S-wave and the $D\pi$ S- and P-waves. For the parameters of broad components, the model uncertainties dominate; however for other parameters the statistical, experimental and model uncertainties are all of a similar magnitude.

The stability of the fit results is confirmed by several cross-checks. The data sample is divided into subsamples according to the flavor of the B candidate, the trigger decision, the polarity of the magnet and the year of data taking. Each subsample is fitted separately and all are seen to be consistent with the nominal fit results. The fit is also repeated with additional resonance components to test the fit model. Resonances up to spin-3 were considered for all three pairs of daughters with the mass and width allowed to vary in the fit. No additional significant contributions were observed.

VIII. RESULTS AND SUMMARY

The results for the complex coefficients are reported in Table VII, with results for the fit fractions given in Table VIII. The results for the interference fit fractions are given in Appendix B. Upper limits are determined on the fit fractions of the $K^*(1410)^0$ and $D_3^*(2760)^-$ components, which do not give significant contributions, using the method described in Ref. [10].

The fit fractions for resonant contributions are converted into quasi-two-body product branching fractions by multiplying by $\mathcal{B}(B^0 \rightarrow \bar{D}^0 K^+ \pi^-) = (9.2 \pm 0.6 \pm 0.7 \pm 0.6) \times 10^{-5}$, which is obtained from the ratio of branching fractions $\mathcal{B}(B^0 \rightarrow \bar{D}^0 K^+ \pi^-) / \mathcal{B}(B^0 \rightarrow \bar{D}^0 \pi^+ \pi^-)$ [15] multiplied by the latest result for $\mathcal{B}(B^0 \rightarrow \bar{D}^0 \pi^+ \pi^-)$ [12], accounting for the different $D^*(2010)^-$ veto windows used in the analyses and for the 3.7% residual background due to $B^0 \rightarrow D^*(2010)^- K^+$ decays. The statistical correlation between the results of Ref. [15] and this analysis is found to

TABLE V. Experimental systematic uncertainties on the fit fractions (%) and masses and widths (MeV). Uncertainties given on the central values are statistical only.

Resonance	Central value	S/B fraction	Efficiency	Background SDP	Fit bias	Total
$K^*(892)^0$	37.4 ± 1.5	0.60	0.83	0.50	0.31	1.17
$K^*(1410)^0$	0.7 ± 0.3	0.06	0.39	0.69	0.05	0.80
$K_0^*(1430)^0$	5.1 ± 2.0	0.28	1.48	1.85	0.33	2.41
LASS nonresonant	4.8 ± 3.8	0.51	2.25	2.86	0.86	3.77
LASS total	6.7 ± 2.7	0.26	1.86	1.60	1.02	2.67
$K_2^*(1430)^0$	7.4 ± 1.7	0.23	0.72	0.53	0.54	1.07
$D_0^*(2400)^-$	19.3 ± 2.8	0.21	1.39	1.43	0.40	2.04
$D_2^*(2460)^-$	23.1 ± 1.2	0.70	0.70	0.49	0.15	1.11
$D\pi$ S-wave (dabba)	6.6 ± 1.4	0.03	0.81	0.59	0.57	1.15
$D\pi$ P-wave (EFF)	8.9 ± 1.6	0.86	1.91	0.52	0.38	2.19
$m(D_0^*(2400)^-)$	2360 ± 15	4.6	8.1	7.0	3.7	12.2
$m(D_2^*(2460)^-)$	2465.6 ± 1.8	0.01	0.37	0.22	0.29	0.51
$\Gamma(D_0^*(2400)^-)$	255 ± 26	2.8	13.1	13.9	4.8	19.9
$\Gamma(D_2^*(2460)^-)$	46.0 ± 3.4	0.5	0.9	0.9	0.5	1.4

TABLE VI. Model uncertainties on the fit fractions (%) and masses and widths (MeV). Uncertainties given on the central values are statistical only.

Resonance	Central value	Fixed parameters	Add/remove	Alternative models	Total
$K^*(892)^0$	37.4 ± 1.5	0.75	1.14	1.09	1.74
$K^*(1410)^0$	0.7 ± 0.3	0.18	0.70	0.22	0.76
$K_0^*(1430)^0$	5.1 ± 2.0	0.79	3.30	0.23	3.40
LASS nonresonant	4.8 ± 3.8	1.10	3.99	5.20	6.65
LASS total	6.7 ± 2.7	0.53	1.42	5.21	5.43
$K_2^*(1430)^0$	7.4 ± 1.7	0.36	1.87	0.56	1.98
$D_0^*(2400)^-$	19.3 ± 2.8	0.55	1.95	7.11	7.40
$D_2^*(2460)^-$	23.1 ± 1.2	0.18	0.73	0.99	1.24
$D\pi$ S-wave (dabba)	6.6 ± 1.4	0.27	1.40	3.46	3.74
$D\pi$ P-wave (EFF)	8.9 ± 1.6	0.31	1.99	2.15	2.95
$m(D_0^*(2400)^-)$	2360 ± 15	6.1	9.3	25.6	27.9
$m(D_2^*(2460)^-)$	2465.6 ± 1.8	0.09	1.05	0.48	1.15
$\Gamma(D_0^*(2400)^-)$	255 ± 26	4.0	18.0	43.5	47.2
$\Gamma(D_2^*(2460)^-)$	46.0 ± 3.4	1.4	0.5	2.4	2.9

TABLE VII. Results for the complex amplitudes and their uncertainties presented (top) in terms of real and imaginary parts and (bottom) in terms of magnitudes and phases. The three quoted errors are statistical, experimental systematic and model uncertainties, respectively.

Resonance	Real part	Imaginary part
$K^*(892)^0$	$-0.00 \pm 0.15 \pm 0.24 \pm 0.34$	$-1.27 \pm 0.06 \pm 0.03 \pm 0.06$
$K^*(1410)^0$	$0.15 \pm 0.06 \pm 0.04 \pm 0.09$	$-0.09 \pm 0.09 \pm 0.18 \pm 0.18$
$K_0^*(1430)^0$	$0.14 \pm 0.38 \pm 0.48 \pm 0.38$	$0.45 \pm 0.15 \pm 0.37 \pm 0.17$
LASS nonresonant	$-0.10 \pm 0.24 \pm 0.16 \pm 0.42$	$0.44 \pm 0.14 \pm 0.17 \pm 0.23$
$K_2^*(1430)^0$	$-0.32 \pm 0.09 \pm 0.15 \pm 0.23$	$-0.47 \pm 0.07 \pm 0.14 \pm 0.15$
$D_0^*(2400)^-$	$-0.80 \pm 0.08 \pm 0.07 \pm 0.22$	$-0.44 \pm 0.14 \pm 0.12 \pm 0.18$
$D_2^*(2460)^-$	1.00	0.00
$D\pi$ S-wave (dabba)	$-0.39 \pm 0.09 \pm 0.09 \pm 0.14$	$0.36 \pm 0.17 \pm 0.14 \pm 0.23$
$D\pi$ P-wave (EFF)	$-0.62 \pm 0.06 \pm 0.03 \pm 0.11$	$-0.03 \pm 0.06 \pm 0.05 \pm 0.10$

Resonance	Magnitude	Phase
$K^*(892)^0$	$1.27 \pm 0.06 \pm 0.03 \pm 0.05$	$-1.57 \pm 0.11 \pm 0.16 \pm 0.27$
$K^*(1410)^0$	$0.18 \pm 0.07 \pm 0.10 \pm 0.11$	$-0.54 \pm 0.21 \pm 0.55 \pm 1.04$
$K_0^*(1430)^0$	$0.47 \pm 0.09 \pm 0.10 \pm 0.14$	$1.27 \pm 0.95 \pm 1.04 \pm 0.81$
LASS nonresonant	$0.46 \pm 0.14 \pm 0.16 \pm 0.29$	$1.79 \pm 0.65 \pm 0.35 \pm 0.69$
$K_2^*(1430)^0$	$0.57 \pm 0.05 \pm 0.04 \pm 0.08$	$-2.16 \pm 0.19 \pm 0.43 \pm 0.43$
$D_0^*(2400)^-$	$0.91 \pm 0.07 \pm 0.06 \pm 0.17$	$-2.64 \pm 0.15 \pm 0.14 \pm 0.23$
$D_2^*(2460)^-$	1.00	0.00
$D\pi$ S-wave (dabba)	$0.53 \pm 0.07 \pm 0.04 \pm 0.14$	$2.40 \pm 0.27 \pm 0.24 \pm 0.44$
$D\pi$ P-wave (EFF)	$0.62 \pm 0.06 \pm 0.04 \pm 0.11$	$-3.09 \pm 0.10 \pm 0.07 \pm 0.17$

be negligible. The results for the product branching fractions are shown in Table IX. For the $K^+\pi^-$ resonances, where the branching fractions to $K\pi$ are known, the product branching fractions are converted to the B decay branching fractions, shown in Table X. The results for $\mathcal{B}(B^0 \rightarrow \bar{D}^0 K^*(892)^0)$ and $\mathcal{B}(B^0 \rightarrow D_2^*(2460)^- K^+) \times \mathcal{B}(D_2^*(2460)^- \rightarrow \bar{D}^0 \pi^-)$ are consistent with, and more precise than, previous measurements [14,16,17].

The masses and widths of the $D_0^*(2400)^-$ and $D_2^*(2460)^-$ states are found to be

$$m(D_0^*(2400)^-) = (2360 \pm 15 \pm 12 \pm 28) \text{ MeV}$$

$$\Gamma(D_0^*(2400)^-) = (255 \pm 26 \pm 20 \pm 47) \text{ MeV}$$

$$m(D_2^*(2460)^-) = (2465.6 \pm 1.8 \pm 0.5 \pm 1.2) \text{ MeV}$$

$$\Gamma(D_2^*(2460)^-) = (46.0 \pm 3.4 \pm 1.4 \pm 2.9) \text{ MeV},$$

TABLE VIII. Results for the fit fractions and their uncertainties (%). The three quoted errors are statistical, experimental systematic and model uncertainties, respectively. Upper limits are given at 90% (95%) confidence level.

Resonance	Fit fraction	Upper limit
$K^*(892)^0$	$37.4 \pm 1.5 \pm 1.2 \pm 1.7$	< 3.2 (3.7)
$K^*(1410)^0$	$0.7 \pm 0.3 \pm 0.8 \pm 0.8$	
$K_0^*(1430)^0$	$5.1 \pm 2.0 \pm 2.4 \pm 3.4$	
LASS nonresonant	$4.8 \pm 3.8 \pm 3.8 \pm 6.7$	
LASS total	$6.7 \pm 2.7 \pm 2.7 \pm 5.4$	< 1.0 (1.1)
$K_2^*(1430)^0$	$7.4 \pm 1.7 \pm 1.1 \pm 2.0$	
$D_0^*(2400)^-$	$19.3 \pm 2.8 \pm 2.0 \pm 7.4$	
$D_2^*(2460)^-$	$23.1 \pm 1.2 \pm 1.1 \pm 1.2$	
$D_3^*(2760)^-$		
$D\pi$ S-wave (dabba)	$6.6 \pm 1.4 \pm 1.2 \pm 3.7$	
$D\pi$ P-wave (EFF)	$8.9 \pm 1.6 \pm 2.2 \pm 3.0$	

where the three uncertainties are statistical, experimental systematic and model systematic, respectively. These are consistent with, though less precise than, recent results from a DP analysis of $B^0 \rightarrow \bar{D}^0 \pi^+ \pi^-$ decays [12]. They also show good agreement with, and have similar precision to, earlier measurements of these quantities [13,37].

In summary, the first amplitude analysis of $B^0 \rightarrow \bar{D}^0 K^+ \pi^-$ decays has been presented, using a data sample corresponding to 3.0 fb^{-1} of pp collision data collected by

the LHCb experiment. A good description of the data is obtained with a model containing contributions from intermediate $K^*(892)^0$, $K^*(1410)^0$, $K_2^*(1430)^0$ and $D_2^*(2460)^-$ resonances, with additional components to describe broad structures in the $K\pi$ S-wave and the $D\pi$ S- and P-waves. The masses and widths of the $D_0^*(2400)^-$ and $D_2^*(2460)^-$ resonances are measured, as are the complex amplitudes and fit fractions for all components included in the amplitude model. The results can be used in conjunction with an analysis of $B^0 \rightarrow DK^+ \pi^-$ decays, where the neutral D meson is reconstructed in final states such as $K^+ K^-$, to measure the CKM unitarity triangle parameter γ [1,2].

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TABLE IX. Results for the product branching fractions. The four quoted errors are statistical, experimental systematic, model and PDG uncertainties, respectively. Upper limits are given at 90% (95%) confidence level.

Resonance	Product branching fraction (10^{-5})	Upper limit (10^{-5})
$K^*(892)^0$	$3.42 \pm 0.13 \pm 0.10 \pm 0.16 \pm 0.40$	< 0.29 (0.34)
$K^*(1410)^0$	$0.07 \pm 0.03 \pm 0.08 \pm 0.07 \pm 0.01$	
$K_0^*(1430)^0$	$0.47 \pm 0.18 \pm 0.22 \pm 0.31 \pm 0.05$	
LASS nonresonant	$0.44 \pm 0.34 \pm 0.34 \pm 0.61 \pm 0.05$	
LASS total	$0.61 \pm 0.25 \pm 0.25 \pm 0.49 \pm 0.07$	< 0.10 (0.11)
$K_2^*(1430)^0$	$0.68 \pm 0.15 \pm 0.10 \pm 0.18 \pm 0.08$	
$D_0^*(2400)^-$	$1.77 \pm 0.26 \pm 0.19 \pm 0.67 \pm 0.20$	
$D_2^*(2460)^-$	$2.12 \pm 0.10 \pm 0.11 \pm 0.11 \pm 0.25$	
$D_3^*(2760)^-$		
$D\pi$ S-wave (dabba)	$0.60 \pm 0.13 \pm 0.11 \pm 0.34 \pm 0.07$	
$D\pi$ P-wave (EFF)	$0.81 \pm 0.15 \pm 0.20 \pm 0.27 \pm 0.09$	

TABLE X. Results for the branching fractions. The four quoted errors are statistical, experimental systematic, model and PDG uncertainties, respectively. Upper limits are given at 90% (95%) confidence level.

Resonance	Branching fraction (10^{-5})	Upper limit (10^{-5})
$K^*(892)^0$	$5.13 \pm 0.20 \pm 0.15 \pm 0.24 \pm 0.60$	< 6.7 (7.8)
$K^*(1410)^0$	$1.59 \pm 0.68 \pm 1.81 \pm 1.59 \pm 0.36$	
$K_0^*(1430)^0$	$0.71 \pm 0.27 \pm 0.33 \pm 0.47 \pm 0.08$	
LASS nonresonant	$0.66 \pm 0.51 \pm 0.51 \pm 0.92 \pm 0.08$	
LASS total	$0.92 \pm 0.38 \pm 0.38 \pm 0.74 \pm 0.11$	
$K_2^*(1430)^0$	$2.04 \pm 0.45 \pm 0.30 \pm 0.54 \pm 0.25$	

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APPENDIX A: CORRELATION MATRICES

The statistical correlations between the complex coefficients, masses and widths determined from the fit to data are given in terms of real and imaginary parts, and in terms of magnitudes and phases in Tables XI, and XII. The correlations are determined using the same sample of simulated pseudoexperiments used to calculate the statistical uncertainties on fit parameters.

TABLE XI. Statistical correlations between the real (x) and imaginary (y) parts of the complex coefficients that are free parameters of the fit. Correlations with the masses (m) and widths (Γ) that are determined from the fit are also included. The correlations are determined from the same sample of simulated pseudoexperiments used to evaluate systematic uncertainties. The labels correspond to (0) $K^*(892)^0$, (1) $K^*(1410)^0$, (2) $K_0^*(1430)^0$, (3) LASS nonresonant, (4) $K_2^*(1430)^0$, (5) $D_0^*(2400)^-$, (6) $D_2^*(2460)^-$, (7) $D\pi$ S-wave (dabba), (8) $D\pi$ P-wave (EFF).

	x_0	y_0	x_1	y_1	x_2	y_2	x_3	y_3	x_4	y_4	x_5	y_5	x_7	y_7	x_8	y_8	m_6	Γ_6	m_5	Γ_5
x_0	1.00	0.14	0.02	0.17	-0.18	0.15	-0.17	0.03	0.39	-0.37	0.16	-0.09	-0.18	-0.29	0.07	-0.37	-0.19	0.02	0.04	0.12
y_0		1.00	-0.06	-0.08	0.09	-0.11	-0.00	0.14	0.03	0.03	0.12	0.13	-0.12	-0.24	0.35	-0.07	0.09	0.12	0.01	-0.04
x_1			1.00	-0.09	-0.08	-0.14	-0.04	0.29	-0.01	0.03	-0.20	0.18	-0.21	-0.31	-0.17	-0.36	-0.08	-0.17	-0.23	0.02
y_1				1.00	0.05	0.34	0.09	-0.01	0.60	-0.39	0.02	-0.03	-0.03	0.07	-0.02	-0.04	-0.16	-0.02	0.07	0.02
x_2					1.00	-0.13	0.81	0.09	0.14	-0.16	-0.15	0.21	0.10	0.13	0.04	-0.15	-0.07	0.01	-0.25	0.01
y_2						1.00	0.08	0.28	0.24	-0.36	-0.13	0.08	-0.04	-0.01	-0.04	0.04	-0.02	-0.01	-0.09	-0.10
x_3							1.00	0.20	0.13	-0.34	-0.10	0.33	-0.08	0.08	-0.04	-0.05	-0.07	-0.03	-0.33	-0.09
y_3								1.00	-0.12	-0.12	-0.51	0.29	-0.34	-0.53	0.09	-0.12	0.09	-0.14	-0.36	0.01
x_4									1.00	-0.53	0.32	-0.10	-0.20	0.03	0.02	-0.27	-0.17	-0.06	0.10	-0.00
y_4										1.00	0.06	-0.09	0.40	0.10	0.14	0.16	0.11	-0.05	0.07	-0.03
x_5											1.00	-0.29	-0.03	0.22	0.02	0.04	-0.08	0.02	0.45	-0.06
y_5												1.00	-0.31	-0.34	0.06	0.03	0.24	-0.14	-0.72	-0.33
x_7													1.00	0.46	0.05	0.10	-0.11	-0.01	0.27	0.17
y_7														1.00	-0.16	0.36	-0.01	0.17	0.32	0.08
x_8															1.00	-0.03	0.01	-0.06	-0.09	-0.14
y_8																1.00	0.29	0.02	0.15	-0.02
m_6																	1.00	0.09	0.01	-0.04
Γ_6																		1.00	-0.03	0.00
m_5																			1.00	0.27
Γ_5																				1.00

TABLE XII. Statistical correlations between the magnitudes (a) and phases (Δ) of the complex coefficients that are free parameters of the fit. Correlations with the masses (m) and widths (Γ) that are determined from the fit are also included. The correlations are determined from the same sample of simulated pseudoexperiments used to evaluate systematic uncertainties. The labels correspond to (0) $K^*(892)^0$, (1) $K^*(1410)^0$, (2) $K_0^*(1430)^0$, (3) LASS nonresonant, (4) $K_2^*(1430)^0$, (5) $D_0^*(2400)^-$, (6) $D_2^*(2460)^-$, (7) $D\pi$ S-wave (dabba), (8) $D\pi$ P-wave (EFF).

	a_0	Δ_0	a_1	Δ_1	a_2	Δ_2	a_3	Δ_3	a_4	Δ_4	a_5	Δ_5	a_7	Δ_7	a_8	Δ_8	m_6	Γ_6	m_5	Γ_5
a_0	1.00	-0.11	-0.08	0.05	0.24	0.03	-0.14	0.04	0.04	0.01	0.21	0.02	0.22	-0.22	0.38	-0.00	-0.04	-0.09	-0.01	0.04
Δ_0		1.00	-0.10	0.12	0.03	0.20	0.14	0.14	-0.01	0.45	-0.05	0.10	-0.08	0.35	-0.07	0.05	-0.22	0.06	0.07	0.09
a_1			1.00	-0.35	-0.25	0.06	0.32	0.01	-0.01	-0.38	0.04	-0.22	-0.06	0.31	0.02	0.24	0.07	-0.18	-0.20	0.01
Δ_1				1.00	0.24	0.15	0.16	0.00	0.14	0.38	-0.18	-0.13	0.16	0.26	0.22	-0.06	-0.09	-0.04	-0.12	0.05
a_2					1.00	0.04	0.11	-0.28	-0.07	0.39	-0.09	0.07	0.27	0.10	0.01	0.01	-0.15	0.04	-0.03	-0.13
Δ_2						1.00	0.15	0.77	-0.20	-0.10	-0.01	0.24	0.09	0.13	0.03	-0.09	0.05	0.01	0.23	-0.10
a_3							1.00	-0.06	0.00	-0.11	0.16	-0.30	-0.12	0.56	0.01	0.12	0.02	-0.07	-0.27	-0.04
Δ_3								1.00	-0.28	-0.19	0.15	0.41	-0.24	-0.08	-0.00	-0.13	0.04	0.02	0.41	0.08
a_4									1.00	0.13	0.05	-0.17	0.14	0.18	-0.00	0.06	0.00	0.14	-0.19	-0.09
Δ_4										1.00	-0.16	0.16	0.17	0.12	0.00	-0.02	-0.19	-0.03	0.03	0.01
a_5											1.00	0.24	-0.26	-0.06	0.11	0.05	-0.07	0.01	0.19	0.39
Δ_5												1.00	-0.00	-0.28	-0.01	-0.20	-0.20	0.15	0.76	0.27
a_7													1.00	-0.01	0.17	-0.06	0.04	0.13	-0.05	-0.24
Δ_7														1.00	-0.12	0.37	0.03	-0.00	-0.27	-0.12
a_8															1.00	-0.04	-0.01	0.04	0.06	0.15
Δ_8																1.00	-0.37	-0.02	-0.33	-0.01
m_6																	1.00	0.09	0.01	-0.04
Γ_6																		1.00	-0.03	0.00
m_5																			1.00	0.27
Γ_5																				1.00

APPENDIX B: RESULTS FOR INTERFERENCE FIT FRACTIONS

The central values of the interference fit fractions are given in Table XIII. The statistical, experimental systematic and model uncertainties on these quantities are given in Tables XIV, XV and XVI.

TABLE XIII. Interference fit fractions (%) from the nominal DP fit. The amplitudes are all pairwise products involving (A_0) $K^*(892)^0$, (A_1) $K^*(1410)^0$, (A_2) $K_0^*(1430)^0$, (A_3) LASS nonresonant, (A_4) $K_2^*(1430)^0$, (A_5) $D_0^*(2400)^-$, (A_6) $D_2^*(2460)^-$, (A_7) $D\pi$ S-wave (dabba), (A_8) $D\pi$ P-wave (EFF). The diagonal elements are the same as the conventional fit fractions.

	A_0	A_1	A_2	A_3	A_4	A_5	A_6	A_7	A_8
A_0	37.4	1.8	-0.0	0.0	0.0	-2.4	-0.2	-2.6	-5.0
A_1		0.7	-0.0	0.0	0.0	-1.1	-0.3	-0.6	-1.1
A_2			5.1	-3.2	-0.0	2.9	1.5	1.6	1.9
A_3				4.8	0.0	-8.4	0.1	2.1	0.2
A_4					7.4	-0.3	-1.0	-1.5	-0.4
A_5						19.3	-0.0	2.8	0.0
A_6							23.1	-0.0	0.0
A_7								6.6	-0.0
A_8									8.9

TABLE XIV. Statistical uncertainties on the interference fit fractions (%). The amplitudes are all pairwise products involving $(A_0) K^*(892)^0$, $(A_1) K^*(1410)^0$, $(A_2) K_0^*(1430)^0$, (A_3) LASS nonresonant, $(A_4) K_2^*(1430)^0$, $(A_5) D_0^*(2400)^-$, $(A_6) D_2^*(2460)^-$, $(A_7) D\pi$ S-wave (dabba), $(A_8) D\pi$ P-wave (EFF). The diagonal elements are the same as the conventional fit fractions.

	A_0	A_1	A_2	A_3	A_4	A_5	A_6	A_7	A_8
A_0	1.5	0.7	0.0	0.0	0.0	0.9	0.4	0.4	0.5
A_1		0.3	0.0	0.0	0.0	0.7	0.3	0.4	0.5
A_2			2.0	2.6	0.0	1.1	0.5	1.5	0.5
A_3				3.8	0.0	3.2	0.4	3.4	0.8
A_4					1.7	0.6	0.1	0.6	0.5
A_5						2.8	0.0	3.1	0.0
A_6							1.2	0.0	0.0
A_7								1.4	0.0
A_8									1.6

TABLE XV. Experimental systematic uncertainties on the interference fit fractions (%). The amplitudes are all pairwise products involving $(A_0) K^*(892)^0$, $(A_1) K^*(1410)^0$, $(A_2) K_0^*(1430)^0$, (A_3) LASS nonresonant, $(A_4) K_2^*(1430)^0$, $(A_5) D_0^*(2400)^-$, $(A_6) D_2^*(2460)^-$, $(A_7) D\pi$ S-wave (dabba), $(A_8) D\pi$ P-wave (EFF). The diagonal elements are the same as the conventional fit fractions.

	A_0	A_1	A_2	A_3	A_4	A_5	A_6	A_7	A_8
A_0	1.2	0.5	0.0	0.0	0.0	2.3	0.2	0.4	0.5
A_1		0.8	0.0	0.0	0.0	0.4	0.8	0.7	0.9
A_2			2.4	3.1	0.0	1.4	2.0	2.6	1.1
A_3				3.8	0.0	3.6	0.2	2.6	0.3
A_4					1.1	2.2	0.2	0.5	1.0
A_5						2.0	0.0	4.0	0.0
A_6							1.1	0.0	0.0
A_7								1.2	0.0
A_8									2.2

TABLE XVI. Model uncertainties on the interference fit fractions (%). The amplitudes are all pairwise products involving $(A_0) K^*(892)^0$, $(A_1) K^*(1410)^0$, $(A_2) K_0^*(1430)^0$, (A_3) LASS nonresonant, $(A_4) K_2^*(1430)^0$, $(A_5) D_0^*(2400)^-$, $(A_6) D_2^*(2460)^-$, $(A_7) D\pi$ S-wave (dabba), $(A_8) D\pi$ P-wave (EFF). The diagonal elements are the same as the conventional fit fractions.

	A_0	A_1	A_2	A_3	A_4	A_5	A_6	A_7	A_8
A_0	1.7	0.8	0.0	0.0	0.0	2.6	0.7	0.8	1.4
A_1		0.8	0.0	0.0	0.0	0.8	0.6	0.8	1.1
A_2			3.4	2.9	0.0	5.8	1.7	3.6	2.7
A_3				6.6	0.0	8.3	0.3	3.5	0.7
A_4					2.0	1.7	0.2	1.2	1.0
A_5						7.4	0.0	4.5	0.0
A_6							1.2	0.0	0.0
A_7								3.7	0.0
A_8									2.9

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